

## Some Anomalies Resolved in Colloid Mobility by Electrodeposition Analysis: Depletion *versus* Turbulence

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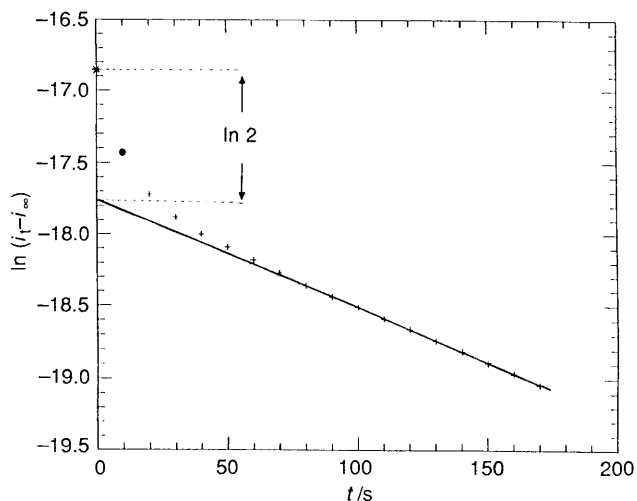
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Since the logarithm of the sol electrodeposition current varies linearly with time (as required by theory) only if uniform composition is maintained by turbulence, a mechanism involving vortical motion is shown to set in after a period and to account for hitherto unremarked 2-fold factors between parameters of the theory, as well as other observations.

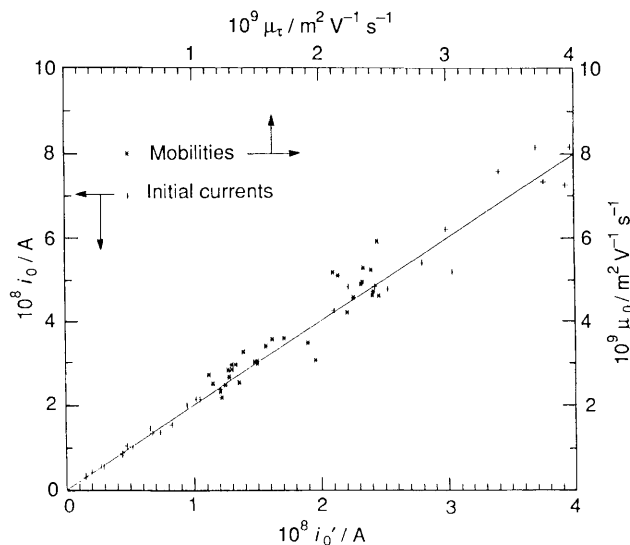
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Colloid mobilities  $u$  are obtained *inter alia* from photon correlation spectroscopy (PCS), or from sol electrodeposition<sup>1</sup> between closely spaced cylindrical electrodes (gap  $L \approx 5$  mm usually). The current  $i$  decay is observed<sup>2</sup> to become logarithmic with time  $t$ , the slope yielding a transit time  $\tau$  for

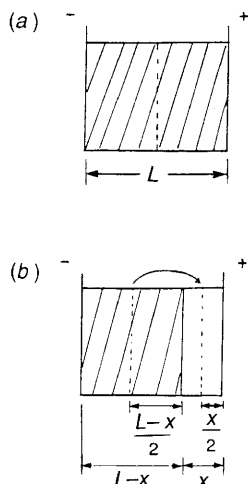
traversal by a typical particle of the distance  $L$ , hence  $u$  may be calculated. The adduced<sup>2</sup> theory, however, rests on unfulfilled diffusion conditions, an initial non-linearity remains unaccounted for, and there is, we find, an unexplained factor of just 2 between the actual initial current  $i_0$  and that logarithmic



**Fig. 1** Plot of  $\ln(i_t - i_\infty)$  against  $t$  (where  $i_\infty$  is small background current) showing 2-fold ratio between back-extrapolated and observed current values at  $t = 0$ , as also seen (without explanation) in seminal paper.<sup>2</sup> (Colloid was carbon black + surfactant  $Zr^{IV}$  mixed-octanoate + acrylic polymer Neocryl B-702 in mixed octane medium.)



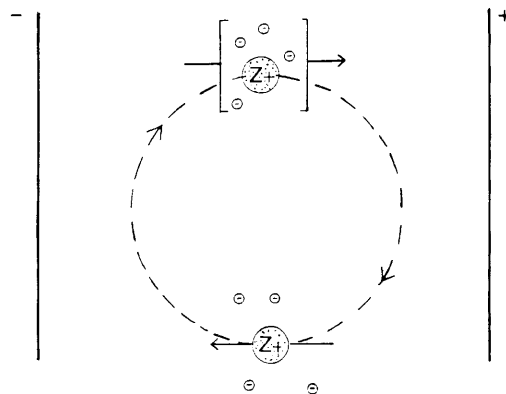
**Fig. 3** Plot of observed  $i_0$  value versus back-extrapolated  $i_0'$  value (both corrected for small background current) for sols as Fig. 1 but of various compositions and at a range of applied potentials. Also, plot of  $u_0$  calculated from  $i_0$  versus  $u_\tau$  from  $\tau$ . Line has a slope of exactly 2.



**Fig. 2** The gap between the electrodes depicted as length  $L$ . (a) Under depletion conditions the average distance traversed<sup>2</sup> is  $L/2$  (all sol material if concentrated in halfway plane, dotted, involves nil net vectorial motion; its transfer then to cathode involves pathlength  $L/2$ ). (b) If depleted region on the right is to be restored to uniform distribution by back-transfer (curved arrow) from the populated region, left, then the extra backward distance is  $L/2$ . One half of the initial population needs to be thus back-transferred to maintain uniformity.

mically back-extrapolated to  $t = 0$ ,  $i_0'$  (Fig. 1). (A related factor 2 also arises between  $u$  values calculated from  $i_0$  and those from  $\tau$ .) We propose a novel mechanism encompassing the observed phenomena which avoids these shortcomings and yields  $u$  values confirmed by PCS.

In summary recapitulation,<sup>3</sup>  $-dn/dt \propto nv = n/\tau$  ( $n$  = particle number density, assumed uniform,  $v = uE$  where  $E$  = field), hence  $n = n_0 \exp(-t/\tau)$ . Given  $i = qvnA$  ( $q$  = average particle charge,  $A$  = electrode area),  $\ln(i/i_0) = -t/\tau$ , as derived.<sup>2</sup> However, for compositional uniformity, the depletion arising from deposition needs to be replenished by diffusion,<sup>2</sup> but since the rate of diffusion, from a simple model, is  $\ll$  rate of migration (by  $\approx 10^3$  fold), this requirement is not met, and compositional uniformity is simply not maintained in the first instance. Instead, a sol-free depletion region grows, extending a distance  $x$ , Fig. 2, from the repelling electrode (anode in our



**Fig. 4** Simplified diagram of mechanism of vortex-controlled motion. The vortex is maintained by the field-driven motion of the (nether)  $Z^+$  sol particle without surrounding anion migration, and in turn effects the counter-field motion of [(upper)  $Z^+$  sol particle plus counterbalancing anions] as [square-bracketed] neutral fluid. Both sol particles move with speed  $v$  towards electrodes. (In a real vortex, many sol particles will be involved, in pro- and anti-field motions in approximately equal number.)

experiments), such depletion being clearly visible in experiments in glass tubes with endface electrodes. In the depletion region, charge-uncompensated anions maintained by the field give rise to a growing counter-field which decelerates the sol particles, giving the sharp initial current fall; the net field at sol particles may decrease as  $\approx 1/x$  or approximately as  $1/t$ , and the consequent linearity expected of  $i$  versus  $\ln t$  is indeed found for the initially decremental excess current.

Growing instability from the free-charge accumulation then results in the convulsive onset of turbulence, which we suggest persists as vortices on the micro scale, a 'circular motion' indeed being observed<sup>3</sup> in sol electrodeposition. This restores uniformity of composition (Fig. 2) and, so, justifies the  $\ln(i)$ ,  $t$  relationship, allowing calculation of  $u$  values which agree with PCS measurements.

The external current up to the onset of turbulence is capacitor-like, the sol deposited being charge-uncompensated (and, in post-deposition short-circuit experiments, slowly releasing *just* the charge so entrapped). With the turbulent convulsion, anions, electrochemically depleted at the anode

by the initial current pulse at  $t = 0$ , are restored in concentration, and in our sols, reactions  $\text{RCO}_2^- \rightarrow \text{RCO}_2^\cdot + \text{e}$ ,  $\text{RCO}_2^\cdot \rightarrow \text{R}^\cdot + \text{CO}_2$  and  $2\text{R}^\cdot \rightarrow \text{R}_2$  ensue.<sup>4</sup> The corresponding cathode electrochemistry involves the metal cation required<sup>5</sup> as a surfactant component attached to sol particles: here  $\text{Zr}^{\text{IV}} + 2\text{e} \rightarrow \text{Zr}^{\text{II}}$  is involved,<sup>6</sup> and neutral solid, now *not* storing charge, is thus deposited.

In restoring uniformity, the turbulence causes the average particle to traverse an *extra* distance  $L/2$  over and above the pathlength, also  $L/2$ , on average traversed under depletion conditions, Fig. 2. This confers the factor 2 on  $i_0/i_0'$ , and on mobilities from  $i_0$  and from  $\tau$ . Both relations are plotted in Fig. 3. Vortical motion giving local turbulence would allow the extra distance to be traversed *via* a backward transport of sol + counter-anion, *i.e.* neutral fluid, on the far side (diametrically opposite, in the vortex, Fig. 4) of current-bearing charge motion by sol particle alone. The former also allows nil-current motion of anions to the anode, to maintain the electrochemistry occurring there.

This interpretation provides for the (late) establishment of uniform composition, the initial logarithmic non-linearity, the

post-deposition charge release, the two 2-fold relationships, a vortical turbulence mechanism for both replenishment and the counter-ion motion required for the electrochemistry, and, additionally, for sol behaviour (the circular motion) in other circumstances. It also provides three virtually independent sources of  $u$ :  $i_0$ ,  $i_0'$  and  $\tau$ , concordance between which (as here) provides strong support for the proposed mechanism.

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